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Apêndice: Otimização usando a Regra de “Iniciar em Zero”

(a) Função Objetivo:

$$\min > \frac{1}{T} \left[\sum_{i=1}^N \frac{h_i}{2} (p_i - r_i) \left(\frac{p_i}{r_i} \right) \sum_{m=1}^M t_m^2 \delta_{im} \right]$$

Substituindo pelos respectivos valores da tabela 4.7, obtém-se:

$$\begin{aligned} \min = & 1 / 6 [6064.2486*(t1^2+t6^2+t11^2+t16^2) + 150252.5778*(t20^2) + \\ & 41915.2965*(t10^2+t19^2) + 10895.0257*(t2^2+t8^2+t12^2+t18^2) + \\ & 716153.0694*(t7^2) + 23758.9701*(t5^2+t15^2) + 486129.6*(t4^2+t14^2) + \\ & 17262.7123*(t3^2+t9^2+t13^2+t17^2)] \end{aligned}$$

Visualmente pode-se mostrar assim:

P1	P2	P3	P4	P5	P6	P7	P8
t1^2							
			t2^2				
							t3^2
						t4^2	
					t5^2		
t6^2							
				t7^2			
			t8^2				
							t9^2
		t10^2					
t11^2							
			t12^2				
							t13^2
						t14^2	
					t15^2		
t16^2							
							t17^2
			t18^2				
		t19^2					
	t20^2						
6064,249	150252,6	41915,3	10895,03	716153,1	23758,97	486129,6	17262,71

(b) Restrições do Tipo:

$$\delta_{im} \left[p_i t_m - r_i \sum_{m'=m}^{m''(m)-1} (t_{m'} + y_{m'} + s_{m'}) \right] = 0, \text{O } m = 1, \dots, M \text{ O } , i = 1, \dots, N$$

- b1) $10500*t1 - 2799 * (t1+0.06944+y1+t2+0.0625+y2+t3+0.08333+y3+t4+0.05556+y4 + t5+0.0625+y5) = 0;$
- b2) $9600*t2-1776*(t2+0.0625+y2+t3+0.08333+y3+t4+0.05556+y4+t5+0.0625+y5+t6+0.06944+y6+t7+0.04167+y7) = 0;$
- b3) $9600*t3-1033*(t3+0.08333+y3+t4+0.05556+y4+t5+0.0625+y5+t6+0.06944+y6+t7+0.04167+y7+t8+0.0625+y8) = 0;$
- b4) $18000*t4-144*(t4+0.05556+y4+t5+0.0625+y5+t6+0.06944+y6+t7+0.04167+y7+t8+0.0625+y8+t9+0.09722+y9+t10+0.05556+y10+t11+0.06944+y11+t12+0.0625+y12+t13+0.08333+y13) = 0;$
- b5) $10500*t5-878*(t5+0.0625+y5+t6+0.06944+y6+t7+0.04167+y7+t8+0.0625+y8+t9+0.09722+y9+t10+0.05556+y10+t11+0.06944+y11+t12+0.0625+y12+t13+0.08333+y13+t14+0.05556+y14) = 0;$
- b6) $10500*t6-2799*(t6+0.06944+y6+t7+0.04167+y7+t8+0.0625+y8+t9+0.09722+y9+t10+0.05556+y10) = 0;$
- b7) $18000*t7-98*(t1+0.06944+y1+t2+0.0625+y2+t3+0.08333+y3+t4+0.05556+y4+t5+0.0625+y5+t6+0.06944+y6+t7+0.04167+y7+t8+0.0625+y8+t9+0.09722+y9+t10+0.05556+y10+t11+0.06944+y11+t12+0.0625+y12+t13+0.08333+y13+t14+0.05556+y14+t15+0.0625+y15+t16+0.08333+y16+t17+0.08333+y17+t18+0.0625+y18+t19+0.04167+y19+t20+0.04167+y20) = 0;$
- b8) $9600*t8-1776*(t8+0.0625+y8+t9+0.09722+y9+t10+0.05556+y10+t11+0.06944+y11) = 0;$
- b9) $9600*t9-1033*(t9+0.09722+y9+t10+0.05556+y10+t11+0.06944+y11+t12+0.0625+y12) = 0;$
- b10) $18000*t10-1563*(t10+0.05556+y10+t11+0.06944+y11+t12+0.0625+y12+t13+0.08333+y13+t14+0.05556+y14+t15+0.0625+y15+t16+0.08333+y16+t17+0.08333+y17+t18+0.0625+y18) = 0;$
- b11) $10500*t11-2799*(t11+0.06944+y11+t12+0.0625+y12+t13+0.08333+y13+t14+0.05556+y14+t15+0.0625+y15) = 0;$

$$b_{12}) 9600 \cdot t_{12} - 1776 \cdot (t_{12} + 0.0625 + y_{12} + t_{13} + 0.08333 + y_{13} + t_{14} + 0.05556 + y_{14} + t_{15} + 0.0625 + y_{15} + t_{16} + 0.08333 + y_{16} + t_{17} + 0.08333 + y_{17}) = 0;$$

$$b_{13}) 9600 \cdot t_{13} - 1033 \cdot (t_{13} + 0.08333 + y_{13} + t_{14} + 0.05556 + y_{14} + t_{15} + 0.0625 + y_{15} + t_{16} + 0.08333 + y_{16}) = 0;$$

$$b_{14}) 18000 \cdot t_{14} - 144 \cdot (t_{14} + 0.05556 + y_{14} + t_{15} + 0.0625 + y_{15} + t_{16} + 0.08333 + y_{16} + t_{17} + 0.08333 + y_{17} + t_{18} + 0.0625 + y_{18} + t_{19} + 0.04167 + y_{19} + t_{20} + 0.04167 + y_{20} + t_1 + 0.06944 + y_1 + t_2 + 0.0625 + y_2 + t_3 + 0.08333 + y_3) = 0;$$

$$b_{15}) 10500 \cdot t_{15} - 878 \cdot (t_{15} + 0.0625 + y_{15} + t_{16} + 0.08333 + y_{16} + t_{17} + 0.08333 + y_{17} + t_{18} + 0.0625 + y_{18} + t_{19} + 0.04167 + y_{19} + t_{20} + 0.04167 + y_{20} + t_1 + 0.06944 + y_1 + t_2 + 0.0625 + y_2 + t_3 + 0.08333 + y_3 + t_4 + 0.05556 + y_4) = 0;$$

$$b_{16}) 10500 \cdot t_{16} - 2799 \cdot (t_{16} + 0.08333 + y_{16} + t_{17} + 0.08333 + y_{17} + t_{18} + 0.0625 + y_{18} + t_{19} + 0.04167 + y_{19} + t_{20} + 0.04167 + y_{20}) = 0;$$

$$b_{17}) 9600 \cdot t_{17} - 1033 \cdot (t_{17} + 0.08333 + y_{17} + t_{18} + 0.0625 + y_{18} + t_{19} + 0.04167 + y_{19} + t_{20} + 0.04167 + y_{20} + t_1 + 0.06944 + y_1 + t_2 + 0.0625 + y_2) = 0;$$

$$b_{18}) 9600 \cdot t_{18} - 1776 \cdot (t_{18} + 0.0625 + y_{18} + t_{19} + 0.04167 + y_{19} + t_{20} + 0.04167 + y_{20} + t_1 + 0.06944 + y_1) = 0;$$

$$b_{19}) 18000 \cdot t_{19} - 1563 \cdot (t_{19} + 0.04167 + y_{19} + t_{20} + 0.04167 + y_{20} + t_1 + 0.06944 + y_1 + t_2 + 0.0625 + y_2 + t_3 + 0.08333 + y_3 + t_4 + 0.05556 + y_4 + t_5 + 0.0625 + y_5 + t_6 + 0.06944 + y_6 + t_7 + 0.04167 + y_7 + t_8 + 0.0625 + y_8 + t_9 + 0.09722 + y_9) = 0;$$

$$b_{20}) 9600 \cdot t_{20} - 158 \cdot (t_1 + 0.06944 + y_1 + t_2 + 0.0625 + y_2 + t_3 + 0.08333 + y_3 + t_4 + 0.05556 + y_4 + t_5 + 0.0625 + y_5 + t_6 + 0.06944 + y_6 + t_7 + 0.04167 + y_7 + t_8 + 0.0625 + y_8 + t_9 + 0.09722 + y_9 + t_{10} + 0.05556 + y_{10} + t_{11} + 0.06944 + y_{11} + t_{12} + 0.0625 + y_{12} + t_{13} + 0.08333 + y_{13} + t_{14} + 0.05556 + y_{14} + t_{15} + 0.0625 + y_{15} + t_{16} + 0.08333 + y_{16} + t_{17} + 0.08333 + y_{17} + t_{18} + 0.0625 + y_{18} + t_{19} + 0.04167 + y_{19} + t_{20} + 0.04167 + y_{20}) = 0;$$

(c) Restrição do Tipo:

$$\sum_{m=1}^M y_m = T \left(1 - \sum_{i=1}^N \frac{r_i}{p_i} \right) - \sum_{m=1}^M s_m$$

$$y_1 + y_2 + y_3 + y_4 + y_5 + y_6 + y_7 + y_8 + y_9 + y_{10} + y_{11} + y_{12} + y_{13} + y_{14} + y_{15} + y_{16} + y_{17} + y_{18} + y_{19} + y_{20} = 0.1372599$$

Para obter os respectivos valores dos t_m 's e y_m 's é preciso resolver as equações formuladas em (a), (b) e (c) através da programação quadrática. Para isto, utiliza-se o Software LINGO 7.0.

No problema apresentado o LINGO 7.0 oferece a seguinte solução:

Local optimal solution found at step:			45
Objective value:			3436.053
Variable	Value	Reduced Cost	
T1	0.3913619	0.0000000	
T6	0.3946870	0.0000000	
T11	0.4054802	0.0000000	
T16	0.4078933	0.0000000	
T20	0.9874962E-01	0.0000000	
T10	0.2559016	0.0000000	
T19	0.2650964	0.0000000	
T2	0.2815626	0.0000000	
T8	0.2744072	0.0000000	
T12	0.3247620	0.0000000	
T18	0.2292639	0.0000000	
T7	0.3266654E-01	0.0000000	
T5	0.2510279	0.0000000	
T15	0.2506844	0.0000000	
T4	0.2401661E-01	0.0000000	
T14	0.2398321E-01	0.0000000	
T3	0.1629993	0.0000000	
T9	0.1650257	0.0000000	
T13	0.1166337	0.0000000	
T17	0.2009638	0.0000000	
Y1	0.2383321E-01	0.1426228E-03	
Y2	0.0000000	258.6804	
Y3	0.0000000	80.18580	
Y4	0.0000000	80.67991	
Y5	0.0000000	85.26003	
Y6	0.0000000	130.9061	
Y7	0.0000000	130.9061	
Y8	0.0000000	66.50996	
Y9	0.0000000	73.29711	
Y10	0.3152697E-01	0.1704633E-03	
Y11	0.6622045E-01	0.0000000	
Y12	0.0000000	233.9683	
Y13	0.0000000	51.88397	
Y14	0.0000000	51.38987	
Y15	0.0000000	46.80975	
Y16	0.0000000	74.46056	
Y17	0.0000000	428.2523	
Y18	0.1567929E-01	-0.1085967E-03	
Y19	0.0000000	73.29683	
Y20	0.0000000	73.29683	

A coluna “*value*” indica os valores que tomam as variáveis (em dias).

O valor da Função Objetivo: 3436.053, representa o custo de manutenção de estoque em uma unidade de tempo (dia). Portanto, o custo por manutenção de estoque no Período de Planejamento H (6 dias) é igual a S/.20616,32.